



## Approaching Effective Parameters of Multi-Trailer Articulated Vehicles in S-Turns with Co-simulation of TruckSim and Taguchi Method

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ARTICLE INFO	ABSTRACT
<b>Article history:</b> Received : 24 April 2019 Accepted: 28 Nov 2019 Published: 1 Dec 2019	Heavy articulated vehicles have low performance with respect to stability analysis due to their multifaceted geometry and dynamics especially when it comes to non-linear maneuvers. In this study in order to find out which statistical and dynamical factors have the most effect on stability of this type of vehicle without getting involve with their complex mathematical theory, combination of drive simulation and Taguchi method is used. Since the number and variety of factors are extensive, multi-step Taguchi method used. This method applied on values of modified rearward amplifications of each units of vehicle as a criterion of lateral stability. Results show the high effect of suspension and load geometry of Vehicle Units on lateral stability and safety
<b>Keywords:</b> Lateral Stability Rearward Amplification Drive Simulation TruckSim Taguchi Method	

### 1. Introduction

Safety is a common concern for all roads users. It is challenged by the traffic density and driving conditions, which have increased substantially over the past years and is expected to continue to rise in the future. Prevention of Multi-Articulated Vehicles (MAV) overturning events is an essential concern too. Only in United Kingdom nearly 60 injury crashes per year involving truck overturns at roundabouts is reported [1]. In a French study, 39 roll-over crashes occurred on 27 roundabouts were analyzed. In 95% of cases, the vehicle was an articulated lorry swiped over outside the ring, on its right side [2]. Most of these crashes are not reported in statistical crash records because they are usually not serious and the speed of involved vehicles is usually low [3]. Nevertheless, these events have economic consequences due to road damage, lorries damage and subsequent traffic disruptions. Langwieder et

al. [4] investigated the benefit of electronic stability control functions in real accident situations involving cars and trucks. The purpose of these control functions was to prevent rollovers and lateral instability [5]. The latter concluded that improving the safety of trucks considerably contributes to road safety as they are involved in 16 % of the fatal accidents. Up to 9 % of the serious accidents involving trucks could have been positively influenced or even prevented with electronic stability control functions. Such functions have already been introduced for tractor semitrailer combinations [6].

Several researchers have considered the influence of the suspension, tires, chassis, and fifth-wheel on the lateral, vertical and longitudinal location, which affects the vehicle dynamic behavior in turnings and maneuvers [7]. Moreno et al. analyzed the last trailer of MAV's, and reported that the static rollover threshold factor represents a three-dimensional phenomenon, and

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that longitudinal parameters and lateral load transfer play important roles in relation to the factor calculation [8]. On the other hand, an improperly loaded trailer can result in a poor trailer stability, overweight on axles, tires deterioration, and damage of the pavement [9]. To calculate the three-dimensional swipe threshold factor for a trailer, the previous work developed a three-dimensional simplified model that considers different characteristics of trailers, such as the suspension, tires, fifth-wheel, chassis and trailer/trailer angle [10]. In these studies for measuring sensitivity and stability (lateral and roll over) are done by using GPS and sensors attached to MAV's body, however their main points went on suspension and geometrical factors [11].

In non-experimental researches Rearward amplification appears to be the dominant performance property distinguishing the yaw response of multi-articulated vehicles from that of other commercial vehicles. This approach has been used in many studies to quantify dynamic behavior of articulated vehicles [12-14]. During transient turning maneuvers, the lateral acceleration of each trailing unit exceeds that of its preceding unit. As a result, the last trailer in a vehicle train has the tendency to swing out excessively which can lead to roll-over [13]. Two methods for calculating the value of rearward amplification are as bellow: 1) rearward amplification is calculated by using lateral accelerations of each unit tails [15], and 2) rearward amplification is defined in the frequency domain as the ratio between the lateral acceleration gains of the last trailer to the towing vehicles front wheel steering angle [16]. Since these studies were experimental and based on quantity of lateral acceleration or frequency amplitude gained by sensors in critical time (depend on lateral safety criterion) they were discrete, so for more precious time line measurement with fine time step is needed.

In conclusion previous researches were lack of two main points. First extensive and variety of MAV's dynamical, statically and geometrical factors must be reconsidered since previous studies absorbed on general ones. Second point goes for a precious and functional method for defining and computing lateral error of units (not only the tail of them) and can be applied even for simulation studies. In the present study, to approach the most effective design parameters including suspension, chassis, tire, and engine factors in S-turn maneuver a specific type of MAV is selected. TruckSim simulation data for proposed vehicle is validated by "Vehicle

Standard Guidelines" [17]. To find rearward amplification value for lateral deviation of tails of each trailer, a new modified method along with Multi-Step Taguchi method apply.

## 2. Approach

In this study a tractor with two articulated trailers jointed by two 5<sup>th</sup> wheel hitches is chosen (Figure 1 B). The application of this type of Ecocomobi is for super heavy loads and it allows having maximum number of hitches (5<sup>th</sup> wheel or other types) and since it has commercial usage in road networks, it can put the travel safety at the high risk [18]. Longer and heavier vehicles have been allowed for many years outside Europe, for example in Australia, South Africa, Mexico, Canada and the USA but it should be noted that Ecocombi's have not been permitted officially in most European countries yet, except Sweden and Finland [19]. Of course there are other combinations and articulations sets but lack of study in two articulated MAVs because of their complex and coupled dynamics give enough reasons to choose this type of MAVs in this study as representative of other multi articulated vehicle.

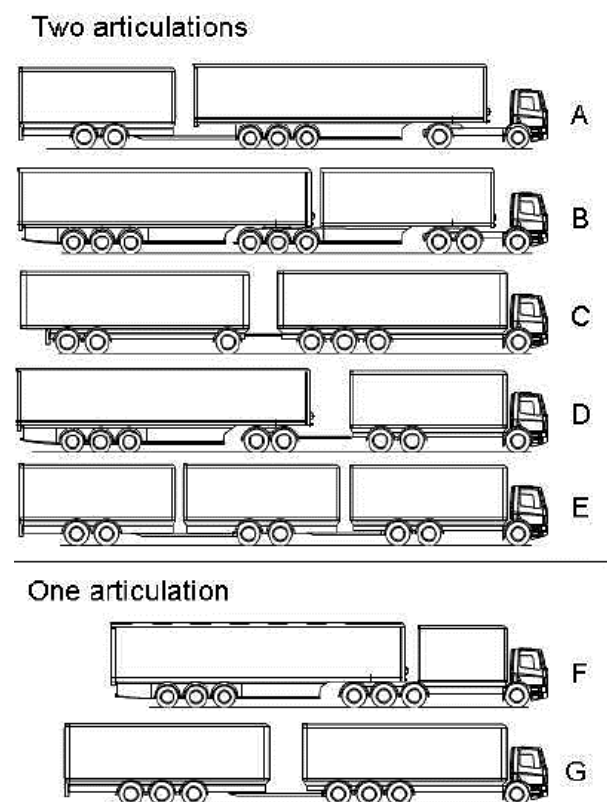


Figure1: One/Two Articulated Vehicles (Ecocombi)

Each unit of the vehicle (Tractor and two Trailers) have their own independent parameters. Since the number of parameters is great enough to handle by applying one step Taguchi Method, it is rational to categorize them into smaller classes. The proper classification in this research is based on two-step Taguchi. In each step effective factors of every mechanical and geometrical parameters tables are selecting by analyzing the SNR result of Taguchi method and top ones of each table form the second step with different boundary value. Boundary value of each parameters in this method are defined my  $6\sigma$  process which will be explained in section 3.2. As it will be discuss later the reason of designing the study in two step of classification and not more is limitation of boundary value of vehicle's parameters which leads to mechanical and physical interference.

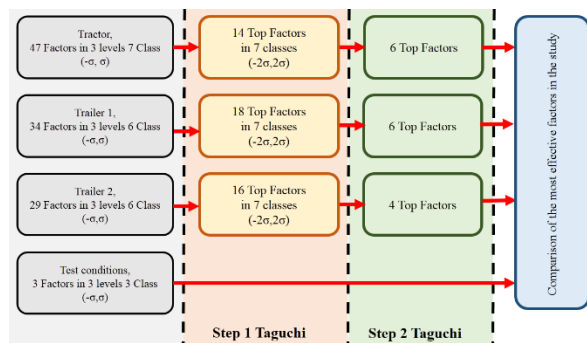


Figure 2 shows an overall view of approach and paper's goal.

Figure 2: Overall View of Approach used in this study.

## 2.1. Parameters Classification of MAV Units

Classification of each unit parameters are based on TruckSim Software configurations which is also follows vehicle's mechanical components and characteristics. Sections 2.1.1 to 2.1.3 describe these categorizations in form of tables for each unit of two articulated vehicle simulated in TruckSim.

### 2.1.1. Tractor Parameters

Tractor parameters according to TruckSim Vehicle Configuration sections are organized in Tables 1-9. Needless to mention all axles used in this study are symmetric.

Table1: Tractor Geometric Parameters

	Factor
1	Sprung Mass of Tractor
2	Height of Tractor
3	Length of Tractor
4	Axle 2 Longitudinal Distance

5	Axle 3 Longitudinal Distance
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Table2: Tractor Tire Parameters

	Factor
1	Tire Type (Touring,Trailer,Truck)

Table 3: Tractor Powertrain Parameters

	Factor
1	Wheel Drive (WD)
2	Powertrain Type
3	Gear Ratio (Axle 1 to 2 and 2 to 3) Open Differential

Table 4: Tractor Hitch Parameters (5<sup>th</sup> wheel)

	Factor
1	Roll stiffness
2	Pitch stiffness
3	Yaw stiffness

Table 5: Tractor Steering Axle 1 Parameters

	Factor
1	Nominal Steering gear ratio (Axle 1)
2	Wheel steering kinematics (Right=Left)
3	Caster Angle (Right=Left)

A Tractor Suspension system of axle 1 is different from axles 2 and 3. Axle 1 is steering system and have air springs while two other axles are driving and leaf springs ones. So, Suspension Kinematics and Compliance Factors are divided to 2 parts.

Table 6: Tractor Axle 1 Suspension Kinematics

	Factor
1	Axle 1 Suspension Kinematic Type
2	Unsprung mass of suspension system
3	Axle roll and yaw inertia
4	Spin inertia for each side
5	Lateral distance between wheels
6	Static toe angles
7	Static Camber angles
8	Dive (Caster) Angles

Table7: Tractor Axle 2 and 3 Suspension Kinematics

	<b>Factor</b>
1	Axle 2 Suspension Kinematic Type
2	Unsprung mass of suspension system
3	Axle roll and yaw inertia
4	Spin inertia for each side
5	Lateral distance between wheels
6	Static toe angles
7	Static Camber angles
8	Axle 3 Suspension Kinematic Type

Table 8: Tractor Axle1 Suspension Compliance

	<b>Factor</b>
1	Suspension Compliance Type (Axle 1)
2	Spring compression/Jounce Ratio (Axle 1)
3	Upper seat height adjustment (Axle 1)
4	Damper force vs compression rate (Axle 1)
5	Stroke (Axle 1)
6	Jounce & Rebound Ratio (Axle 1)
7	Auxiliary Roll Moments (Axle 1)
8	Auxiliary roll damping (Axle1)

Table 9: Tractor Axle 2and 3 Suspension Compliance

	<b>Factor</b>
1	Suspension Compliance Type (Axle 2&3)
2	Spring compression/Jounce Ratio (Axle 2&3)
3	Upper seat height adjustment (Axle 2&3)
4	Damper force vs compression rate (Axle2&3)
5	Stroke (Axle 2&3)
6	Jounce & Rebound Ratio (Axle 2&3)
7	Auxiliary Roll Moments (Axle 2&3)
8	Auxiliary roll damping (Axle2&3)

### 2.1.2. Trailer 1 Parameters

Likewise previous section, Trailer 1 parameters according to TruckSim Vehicle Configuration sections are organized in Tables 10-15. No need to mention that unlike Tractor Unit, the 3 axles of Trailers are identical in properties.

Table 10: Trailer 1 Geometric Parameters

	<b>Factors</b>
1	Height of CG unladen Trailer Bed
2	Height of Hitch point of Trailer Bed
3	Sprung mass of Trailer Bed
4	Longitudinal Distance of CG Trailer Bed
5	Length of Trailer Bed
6	Axle 1 Longitudinal Distance
7	Axle 2 Longitudinal Distance
8	Axle 3 Longitudinal Distance

Table 11: Trailer 1 Tire Parameters

	<b>Factors</b>
1	Tire Type (same for all/Duality)
2	Tire Space of Duality (all same)

Table12: Trailer 1 Hitch Parameters (5<sup>th</sup> wheel)

	<b>Factor</b>
1	Roll stiffness
2	Pitch stiffness
3	Yaw stiffness

Table 13: Trailer 1 Suspension Kinematics Parameters

	<b>Factors</b>
1	Dynamic Load transfer coefficients
2	Suspension Kinematics Type (All axles are same)
3	Unsprung mass of suspension
4	Axle roll and yaw inertia
5	Spin Inertia for each side
6	Lateral Distance between wheels of axle
7	Static toe angle
8	Static Camber angle
9	Caster Angle Type

Table 14: Trailer 1 Load Parameters

	<b>Factors</b>
1	Height of Load
2	Mass of the Load
3	Longitudinal Distance Load CG

Table 15: Trailer 1 Suspension Compliance Parameters

	<b>Factors</b>
1	Suspension Compliance Type
2	Spring compression/Jounce Ratio
3	Upper seat height adjustment
4	Damper force vs compression rate
5	Damper compression/Jounce Ratio
6	Stroke
7	Jounce & Rebound Ratio
8	Auxiliary Roll Moments
9	Auxiliary roll damping

### 2.1.3. Trailer 2 Parameters

Similar to Trailer1, Trailer2 parameters according to TruckSim Vehicle Configuration sections are structured in Tables 16-20.

Table 16: Trailer 2 Geometric Parameters

	<b>Factors</b>
1	Height of CG unladen Trailer Bed
2	Height of Hitch point of Trailer Bed
3	Sprung mass of Trailer Bed
4	Longitudinal Distance of CG Trailer Bed
5	Length of Trailer Bed
6	Axle 1 Longitudinal Distance
7	Axle 2 Longitudinal Distance
8	Axle 3 Longitudinal Distance

Table 17: Trailer 2 Tire Parameters

	<b>Factors</b>
1	Tire Type (same for all/Duality)
2	Tire Space of Duality (all same)

Table 18: Trailer 2 Suspension Kinematic Parameters

	<b>Factors</b>
1	Dynamic Load transfer coefficients
2	Suspension Kinematics Type (All axles are same)
3	Unsprung mass of suspension
4	Axle roll and yaw inertia
5	Spin Inertia for each side
6	Lateral Distance between wheels of axle
7	Static toe angle
8	Static Camber angle

Table 19: Trailer 2 Load Parameters

	<b>Factors</b>
1	Height of Load
2	Mass of the Load
3	Longitudinal Distance Load CG

Table 20: Trailer 2 Suspension Compliance Parameters

	<b>Factors</b>
1	Suspension Compliance Type
2	Spring compression/Jounce Ratio
3	Upper seat height adjustment
4	Damper force vs compression rate
5	Damper compression/Jounce Ratio
6	Stroke
7	Jounce & Rebound Ratio
8	Auxiliary Roll Moments
9	Auxiliary roll damping

## 3. Method

Before Applying Multi-Step Taguchi, Number of Levels, their value boundary for each Factors and a new modified method for calculation of rearward amplification must be set.

### 3.1. Modified Rearward Amplification

As it was explained briefly, Rearward Amplification (RA) seems to be the dominant performance property distinguishing the yaw response of multi-articulated vehicles from that of other commercial vehicles. It has been used in many studies to quantify the dynamic behavior of articulated vehicles. Two Methods of calculating RA are common in literature. In the first Method, rearward amplification is calculated by using maximum value of lateral accelerations at each unit's tail, which presents in equation [20] (1):

$$RA_t = \frac{Max(abs(a_{yn}))}{Max(abs(a_{y1}))} \quad (1)$$

The second method defines rearward amplification in the frequency domain as the ratio between the lateral acceleration gains of the last trailer to the towing vehicle's front wheel steering angle. In other word, in the second definition for rearward amplification the lateral acceleration due to steering wheel angle  $H_{ay_n, \delta_1} = \left| \frac{a_{yn}}{\delta_1} \right|$ , and the lateral acceleration due to steering wheel angle

gained by the towing vehicle  $H_{ay_1, \delta_1} = \left| \frac{a_{y1}}{\delta_1} \right|$  are used [21]. Equation (2) shows formulation of this method:

$$RA_f = \max \left| \frac{H_{ay_n, \delta_1}}{H_{ay_1, \delta_1}} \right| \quad (2)$$

In these methods, depending on MAV's Type (Figure 1) and road conditions, Value of RA has critical boundary, which if the absolute value of rearward amplification exceeds, it will be considered as failure and crash. Figures 3 and 4 show the maximum allowable rearward amplification of MAV with 2 trailers in dry road condition for both mentioned methods [20].

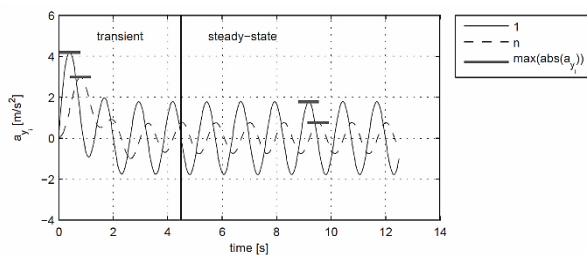


Figure3: Maximum Allowable rearward amplification by First Method;  $RA_t = 1.4$

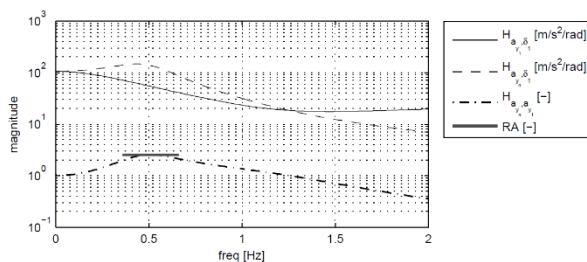


Figure4: Maximum Allowable rearward amplification by Second Method;  $RA_f = 2.5$

The second method based on analyzing of Frequency Response Function (FRF) which requisite the definition of motion equations, state space matrices and leave it to the MATLAB System Identification Toolbox. This method however is more accurate and its initial data are more accessible for this research, but depending on the number of freedom degree of modeling and linearization in simulation study bring errors in calculating rearward amplification value.

The new modified method is based on the second method. But by using TruckSim real-time Simulator software which simulate the MAV non-linear and independent of its freedom degree of modeling, one can have more accuracy in computing lateral accelerations and steering angles. Since in S-turn maneuver lateral accelerations of trailers fluctuate, the rearward amplification value computes through equation 2

for every 0.01s (Minimum available time step of TruckSim simulation).

Similar to previous studies, this method has its own critical boundary name  $RA_s$ . For the test conditions in this research, the safe  $RA_s$  boundary is:

$$1 \leq RA_s \leq 2.5 \quad (3)$$

$RA_s=1$  indicates the situations when units are aligned and it's the research target. Due to standard road width (3m) and maximum allowable hitch orientation angle to avoid jackknifing (60 Degree), if RA exceeds 2.5 it will assume as failure and crash [17]. To apply Taguchi method for each test, a numerical value is needed to express the deviation error of rearward amplifications from  $RA_s = 1$  as criterion. To find out deviation error or similarity of two vector of arrays dozens of methods have been proposed and applied in mathematical and genetics fields [22]. Most of these methods based on giving a percentage value of having 0 or 1 for being different or exact similar respectively. These methods cannot be applied in this study since having identical value between i-th number two arrays (Vector  $RA_s=1$  and Unit's  $RA_s$  Vector during the path) are almost zero. So in this study "Pairwise distance between two sets of observations" methods, in precise "Euclidean distance" method apply which one can function it by "D=pdist2" command in MATLAB [23]. With this command similarity or deviation error of these vectors results as format of one number (Called "D" Value) and operational to apply for Taguchi method's goal column. Figures 5-6 and Table 21 brings the results of running an example test to clarify the process discussed above.

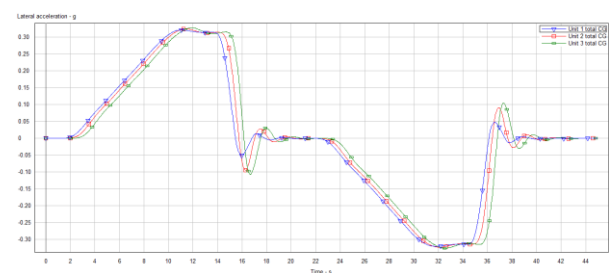


Figure5: Lateral Acceleration of CG's Units for an example Test

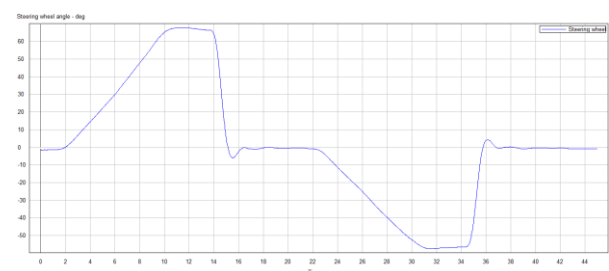


Figure6: Steering front wheel angle for an example Test

Table 21: Results of Unit's RA and Calculation of "D" Value for 10 time step

	$a_y$ Unit 3 (g)	$a_y$ Unit 2 (g)	$a_y$ Unit 1(g)	Steering Wheel Angle (deg)	Max $RA_s$	Target $RA_s=1$
1	0.001	0.0009	0.0007	2	1.4285	1
2	0.021	0.0189	0.0157	4.58	1.3375	1
3	0.041	0.0369	0.0307	7.16	1.3355	1
4	0.061	0.0549	0.0457	9.74	1.3347	1
5	0.081	0.0729	0.0607	12.32	1.3344	1
6	0.101	0.0909	0.0757	14.9	1.3342	1
7	0.121	0.1089	0.0907	17.48	1.3340	1
8	0.141	0.1269	0.1057	20.06	1.3339	1
9	0.161	0.1449	0.1207	22.64	1.3338	1
10	0.181	0.1629	0.1357	25.22	1.3338	1
<b>D = 1.322</b>						

3.2. Levels Design

Back to parameter classification section, classes have 1 to 9 factors. Due to limitation of MINITAB program for Taguchi designing, 3 levels are the utmost steps it can be considered. To find a proper data interval for levels in each factor, Tolerance Interval Tool in MINITAB software applied. As an example, Factor "Longitudinal Distance between Axles" for proposed vehicle can vary between 0.1m to 1.3m due to Vehicle Standard Guideline [17]. By considering (0.1, 1.3) as lower and upper boundary value for this factor and proceeding Tolerance Interval Tool, 6 $\sigma$  intervals yield. It's important to mention that number and their value of data use between the interval boundaries of each factor are arbitrary. Note that for factors which enough data can not be accessible through manufacture's guidelines to build intervals are conceded to TruckSim application. In this research (- $\sigma$ ,  $\sigma$ ) and (-2 $\sigma$ , 2 $\sigma$ ) intervals applied for first and second step of Taguchi respectively. Table 22 and figures 7 show the results of this example. (Mark \* represent the default value)

Table22: Example longitudinal distance between Trailer's Axles Interval and related D Value

	Longitudinal distance between Trailer's Axles (m)	D Value
1	0.1	0.512
2	0.2	0.600
3	0.5	0.650
4	1	1.000
5	1.1	1.012
6	1.2	1.110

7	1.27*	1.220
8	1.3	1.530

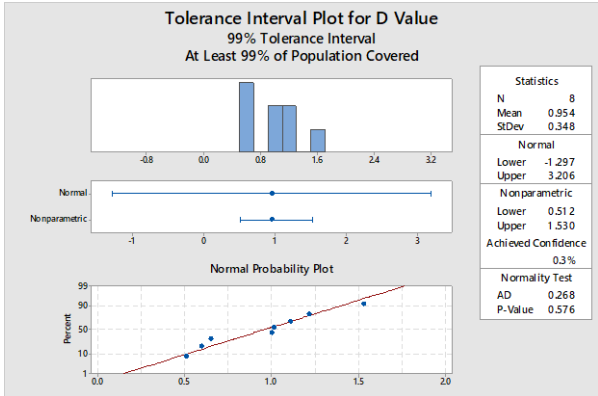


Figure 7: Tolerance Interval plot for D Value

Referring to Figure 7, (- $\sigma$ ,  $\sigma$ ) and (-2 $\sigma$ , 2 $\sigma$ ) interval of D value are equal to (0.606, 1.32) and (0.258, 1.65). Longitudinal Distance of Axles intervals related to these D values are (0.19, 1.275) and (N/A, N/A). N/A occurs when related interval for factors interfere with vehicles dynamics or design guidelines.

3.3. Test Conditions

In order to find the effect of driving and test conditions, a one-step Taguchi process applied. Levels are designed base on JASO (Japanese Standard Organization) program for heavy vehicles [24]. The \* mark in table 23 resembles default road and driving condition in TruckSim Simulator.

Table 23: Test Conditions Levels

	Level 1	Level 2	Level 3
Test Speed	30 Km/h	50 Km/h	*80 Km/h
Road Friction	0.2	0.5	*0.85
Bank Degree	*0 Deg	10 Deg	20 Deg

4. Results

The results of applying the first and second step of Taguchi's Method for each unit parameters classes are presented in sections 4.1 to 4.3.

4.1. Tractor Unit Results

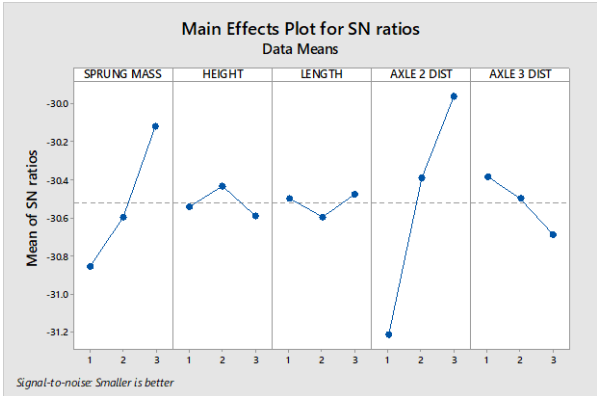


Figure8: First Step Taguchi for Geometric Factors

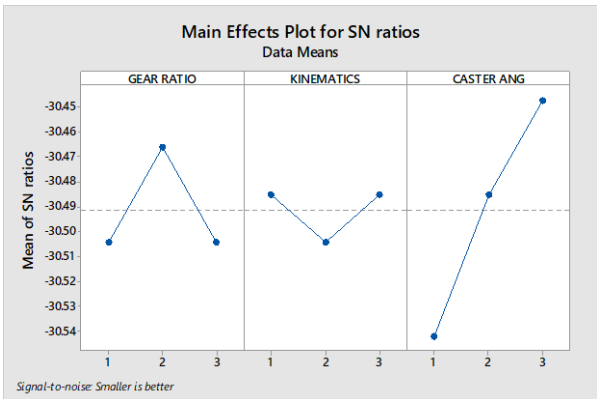


Figure9: The First Step Taguchi for Powertrain Factors

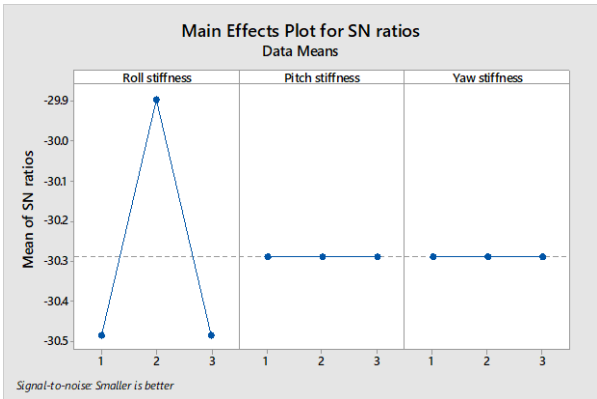


Figure10: First Step Taguchi for Hitch Factors

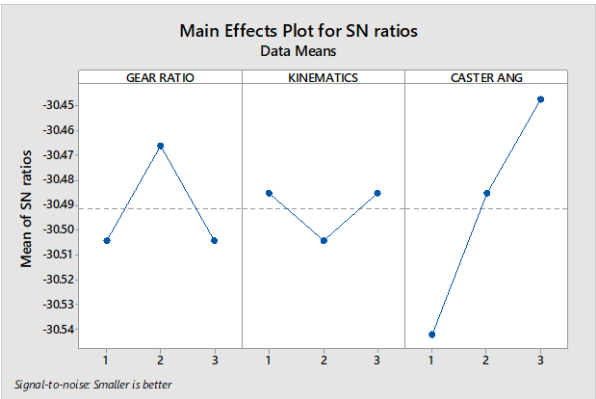


Figure11: First Step Taguchi for Steering Factors

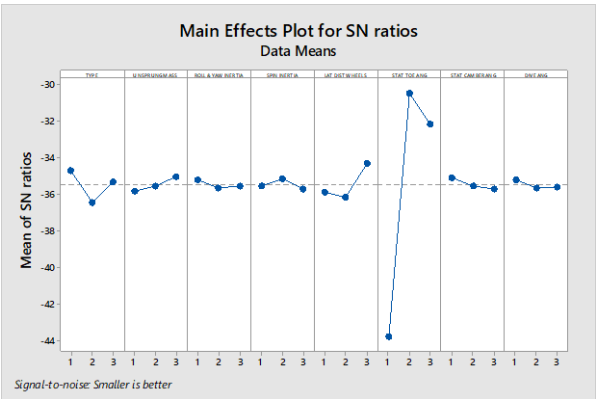


Figure12: First Step Taguchi for Suspension Kinematics of Axle 1

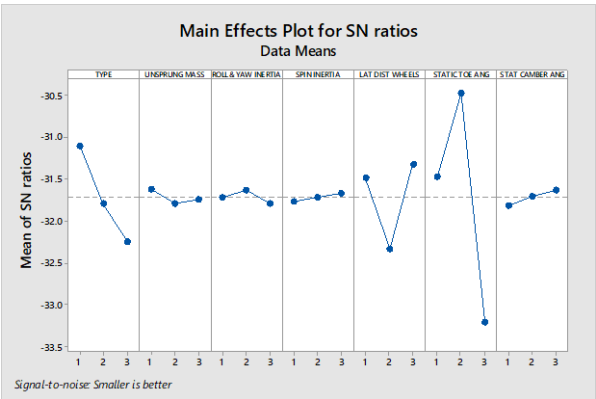


Figure13: The First Step Taguchi for Suspension Kinematics of Axles 2 and 3.

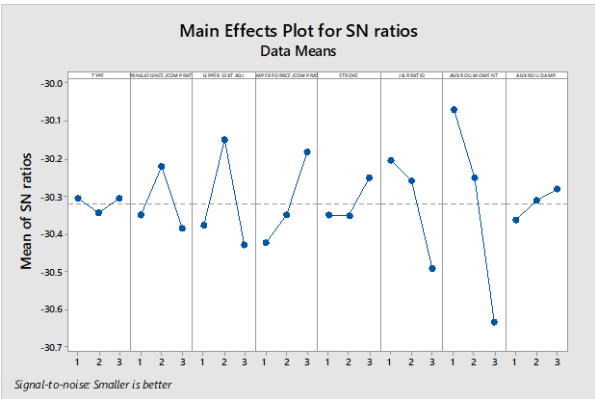


Figure14: First Step Taguchi for Suspension Compliance of Axle 1

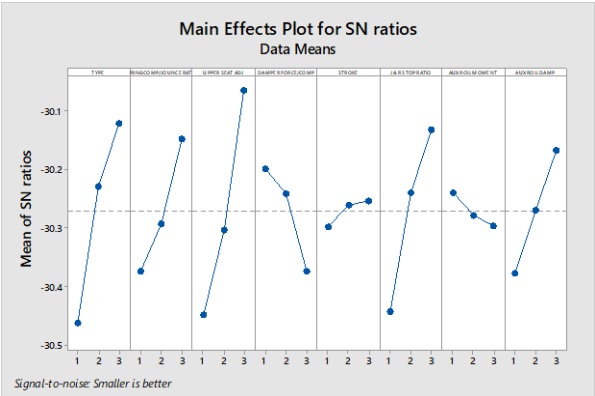


Figure15: First Step Taguchi for Suspension Compliance of Axles 2 and 3

No need to mention Tire Parameters consist of only one factor, so Taguchi Method didn't apply and consider it for the next step. Effective Factors of each class are represented in Table 24.

Table 24: Effective Factors of the First Step Taguchi for Tractor Unit

No.	Class	Tops
1	Geometry Factors	Sprung mass
		Axle 2 Distance
		Axle 3 Distance
2	Tire Factors	Types
3	Powertrain Factors	WD
4	Hitch Factors	Type
		Roll Stiffness
		Toe angle
5	Suspension kinematics Factors	Lateral distance between the wheels
		Type
		Damper force /compression ratio for axles
6	Suspension compliance Factors	

		Axle Type
		Jounce and rebound stop ratio for axles
7	Steering Factors	Caster Angles

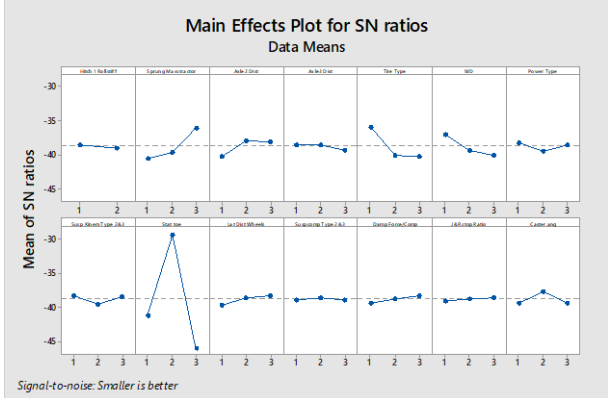


Figure16: Second Step Taguchi for Effective Factors of the First Step.

Table 25: Effective Factors of Second Step Taguchi for Trailer Unit

	Class	Factor
1	Geometry Factors	Sprung Mass
2	Tire Factors	Tire Type
3	Suspension Kinematic Factors	Type
		Toe Angle
4	Powertrain Factors	WD
5	Steering Factors	Caster Angle

## 4.2. Trailer 1 Unit Results

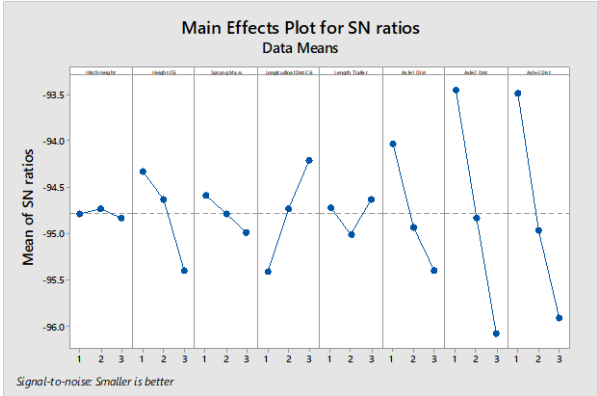


Figure17: The First step Taguchi for Geometric Factors

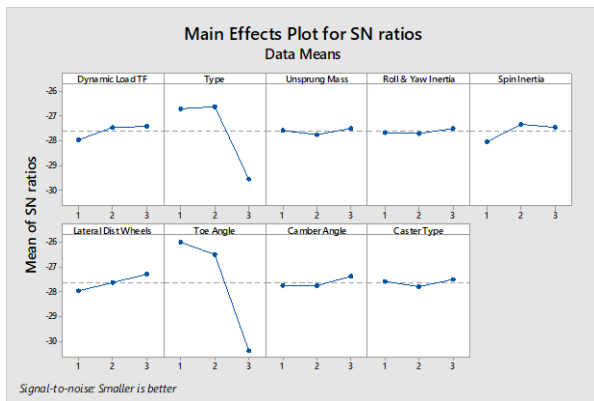
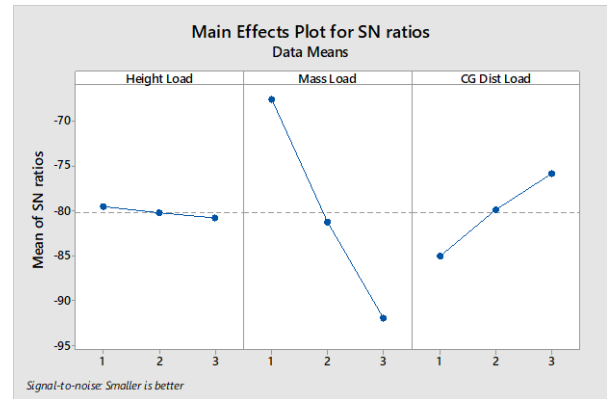
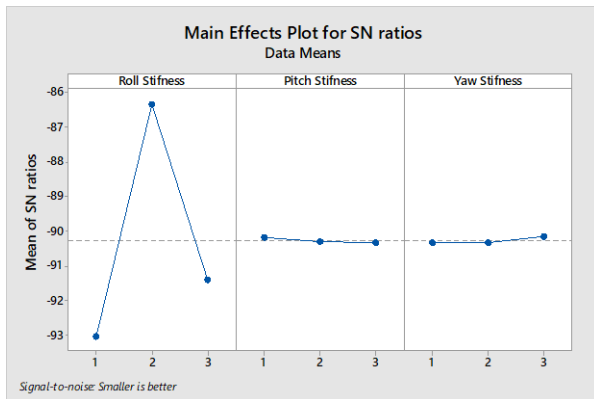
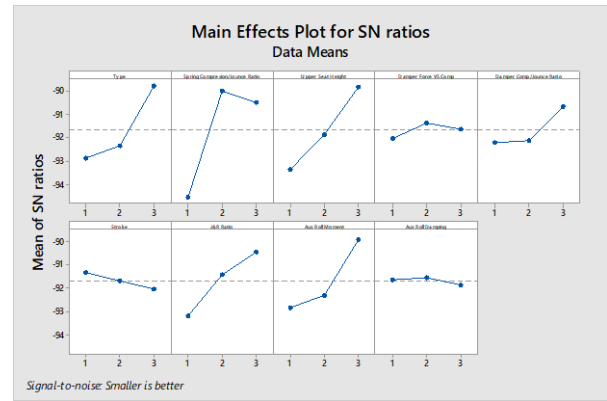
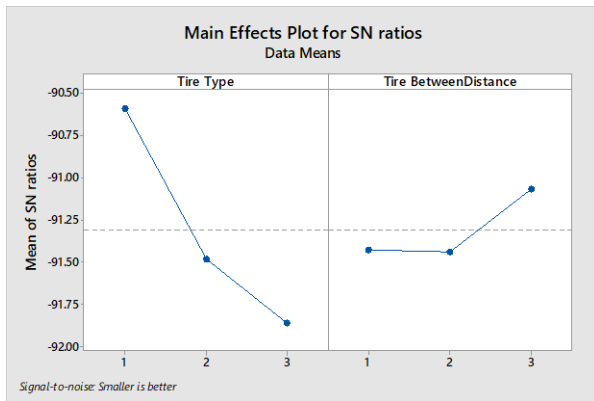


Table 26: Effective Factors of the First Step Taguchi for Trailer 1 Unit

	Class	Effective Factors
1	Geometry Factors	Height of CG unladen Trailer Bed
		Sprung mass of Trailer Bed
		Longitudinal Distance of CG Trailer Bed
		Axle 1 Distance
		Axle 2 Distance
		Axle 3 Distance
2	Tire Factors	Tire Type
3	Hitch Factors	Hitch 2 Roll stiffness (5 <sup>th</sup> wheel)
4	Suspension Kinematics Factors	Suspension Kinematics Type
		Static toe angle (L=R)
5	Suspension Compliance Factors	Suspension Compliance Type
		Spring compression/Jounce Ratio
		Upper seat height adjustment
		Damper compression/Jounce Ratio

6	Load Factors	Jounce & Rebound Ratio
		Auxiliary Roll Moments
		Mass of the Load
		Mass Center of Load

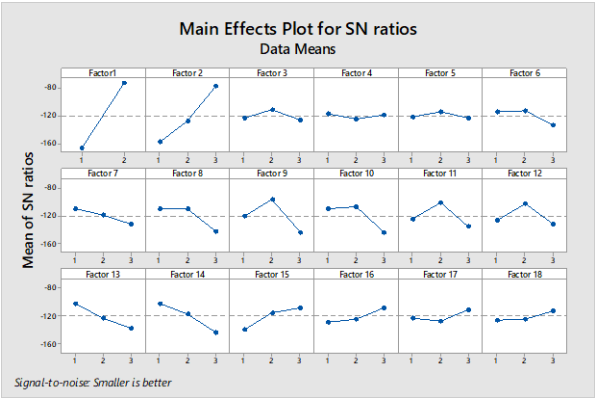


Figure23: Second Step Taguchi for Effective Factors of the First Step

Table 27: Effective Factors of Second Step Taguchi for Trailer 1 Unit

	Class	Effective Factors
1	Geometry Factors	Height of CG unladen Trailer Bed
		Axle 3 Distance
2	Tire Factors	Tire Type
3	Hitch Factors	Hitch 2 Roll stiffness (5 <sup>th</sup> wheel)
4	Suspension Kinematics Factors	Suspension Kinematics Type
		Static toe angle (L=R)
5	Suspension Compliance Factors	Suspension Compliance Type
		Spring compression/Jounce Ratio
6	Load Factors	Mass of the Load
		Mass Center of Load

4.3. Trailer 2 Unit Results

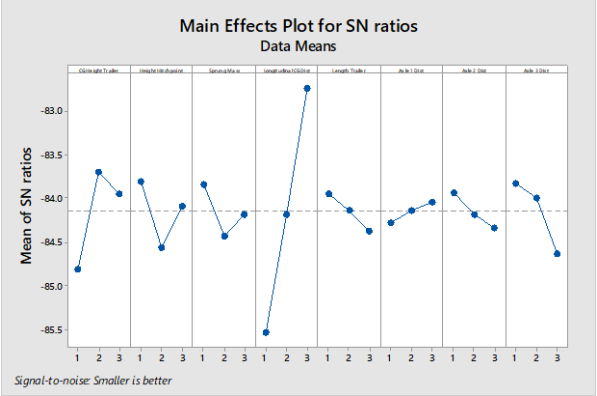


Figure24: The First Step Taguchi for Geometric Factors

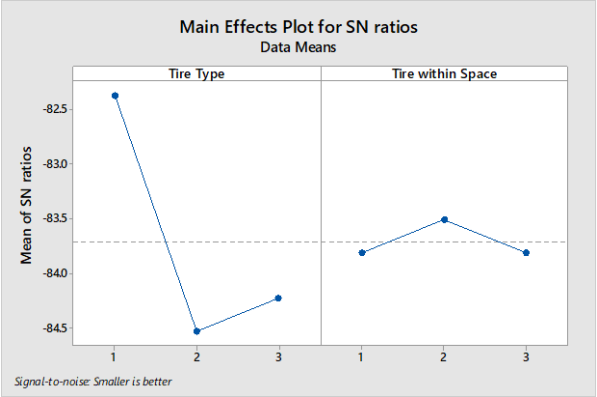


Figure25: First Step Taguchi for Tire Factors

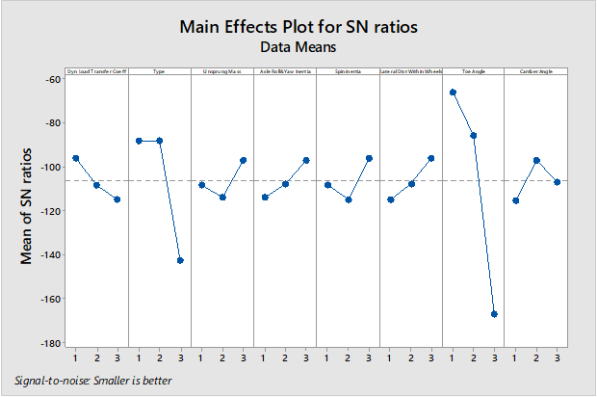


Figure26: First Step Taguchi for Suspension Kinematic Factors

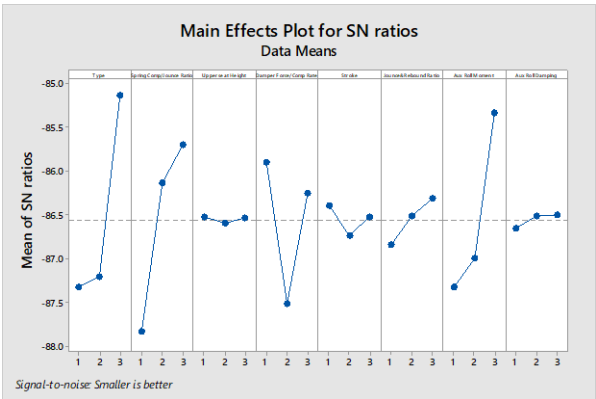


Figure27: First Step Taguchi for Suspension Compliance Factors

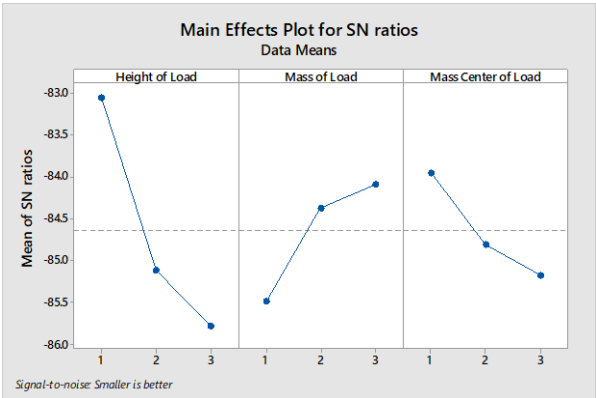


Figure28: The First Step Taguchi for Load Factors

Table 28: Effective Factors of First Step Taguchi for Trailer 2 Unit

	Class	Factors
1	Geometry Factors	Longitudinal Distance of CG Trailer Bed
		Height of CG unladen Trailer Bed
		Axle 3 Distance
2	Tire Factors	Tire Type
3	Suspension Kinematics	Dynamic Load Transfer Coefficient
		Suspension Kinematic type
		Toe Angle
		Lateral Distance within wheels
		Axles Roll & Yaw Inertia
4	Suspension Compliance	Suspension Compliance Type
		Spring Compression/Jounce Ratio
		Damper Force/Compression Rate

		Auxiliary Roll moment
5	Load Factors	Height of Load
		Mass of the Load
		Mass Center of Load

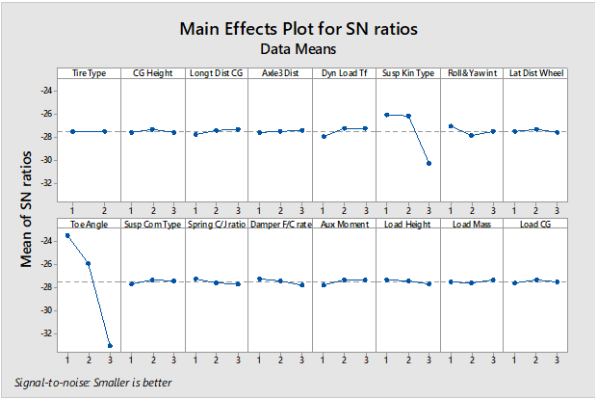


Figure29: Second Step Taguchi for Effective Factors of First Step

Table 29: Effective Factors of Second Step Taguchi for Trailer 2 Unit

	Class	Factor
1	Suspension Kinematics	Dynamic Load Transfer Coefficient
		Toe Angle
		Suspension Kinematic type

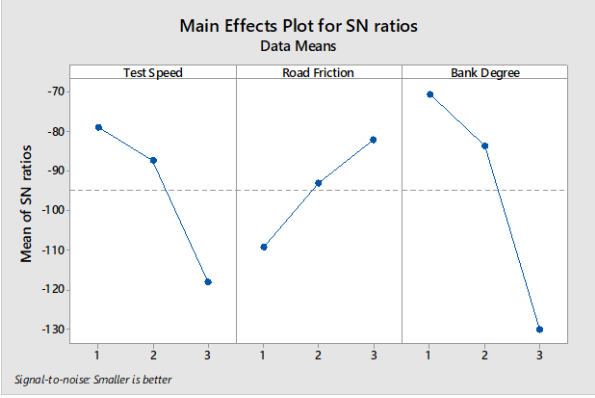


Figure30: Taguchi for Test Conditions

5. Discussion

The results of this study shows that Suspension parameters (Kinematics and compliance) are the most effective factors in rearward amplifications for each units and Geometric, Tire factors, and Load conditions stand in the second and third places respectively.

The Effects of Geometric, Load and Tire factors had been studied in details before [25],[11], but since studying suspension factors needs experimental or simulation tests it has not been covered properly since this study. As it was

explained in section 3.1, the reason of limit founding in past studies was modeling MAVs based on linear and specific number of freedom degree that researcher applied for physical and geometrical parameters to reach state space matrix. Reviewing the latest researches a list of effective factors on RA value is given in Table 30. [25].

Table 30: Effective Factors studied in Latest papers

	Factors
1	CG Distance of Loads
2	neutral steer parameters
3	lengths of the units
4	Hitch Distance
5	Length between the axles
6	Height of the Load and Tractor
7	Speed of Vehicle
8	Road Friction

As it can be concluded mostly previous works didn't study the major effects of Suspension and other cited parameters, outcome in this study and that's the nobility of this research. In addition, the effects of test conditions are covered, and as can be derived bank degree of road has the first place and the two others in further have effective roles.

## 6. Conclusion

In this study in order to find the most effective factors of a specific and common MAV among tons of its statistical and dynamical parameters, multi-step Taguchi method applied as main process. Due to limitation of experimental test and its cost, TruckSim Simulator software which offered real time, non-linear and accurate studies were selected. After representing 6 $\sigma$  method for designing levels of factors variety in each step of Taguchi, a modified rearward amplification method was presented to compute deviation error of RA value for each unit from its criterion. After applying 2-step Taguchi for parameters of each unit, results concluded that factors like suspension's angle, tire type and bank degree of the road which had major effects, must be listed beside the geometric and load factors that had been study before.

Involving with these most effective factors instead of working tons of MAV's parameters in hard maneuvers driving conditions for body designing, controlling studies and optimization for further researches can be huge help [26].

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